



Accelerators and particle detectors

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Phenomenology of Particle Physics - HS2010

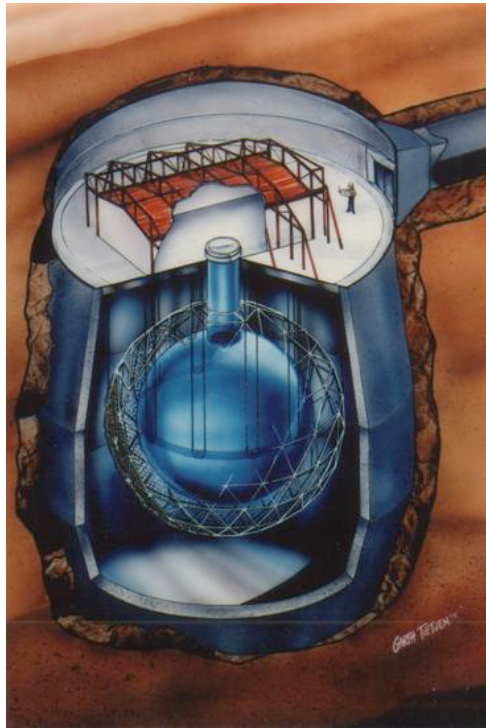
Lectures: 1-2 November 2010

Lectures outlook

- Introduction to particle accelerators and detectors
 - ◆ Basic principles of particle accelerators
 - ◆ Fixed target and collider experiments
 - ◆ Center of mass energy
 - ◆ Luminosity, Cross section, Event rates
 - ◆ Basic building blocks of a particle physics experiment
 - ◆ Momentum measurement
- Data analysis tools and kinematics:
 - ◆ Rapidity
 - ◆ Momentum conservation:
 - Transverse momentum, missing momentum
 - ◆ Invariant mass

Introduction

- Modern techniques in experimental particle physics can be divided into:
 - ◆ **Non accelerator-based** experiments
 - Examples: Cosmic rays, solar and atmospheric neutrinos, searches for dark matter
 - ◆ **Accelerator-based** experiments
 - Example: fixed target experiments, particle colliders



Particle accelerators: motivations

- Fundamental tool for research in physics
- Main parameter is the **beam energy**:
 - ◆ More energy → **Shorter wavelength**
 - Can investigate structures with size $\lambda=h/p$.
 - ◆ More energy → **Can produce new particles**
- Accelerate beam of stable particles (e.g. protons, anti-protons, e^+ , e^-)
- Applications of a particle accelerator:
 - ◆ Collide with other beams and study resulting interactions
 - ◆ Collide against a fixed target
 - Study resulting interactions
 - Produce a secondary beam of particles (stable, unstable, charged, neutral) for a subsequent collision

Particle accelerators: motivations

- Search for new sub-structures:
 - ◆ De-Broglie equation: $\lambda=h/p$. Increases resolving power at higher energies.
 - ◆ $p=1 \text{ GeV}/c \rightarrow \lambda=1.24 \cdot 10^{-15} \text{ m}$
 - ◆ $p=10^3 \text{ GeV}/c \rightarrow \lambda=1.24 \cdot 10^{-18} \text{ m}$
- Search for new particles with high mass:
 - ◆ Example: collision in the laboratory frame between two particles: (m_1, \mathbf{p}_1) and (m_2, \mathbf{p}_2)

$$E_L = \sqrt{p_1^2 + m_1^2} + \sqrt{p_2^2 + m_2^2} \quad p_L = |\vec{p}_1 + \vec{p}_2|$$
$$\boxed{E_L^2 - p_L^2 = E_{CM}^2 - p_{CM}^2} \quad \Rightarrow \quad E_{CM} = \sqrt{E_L^2 - p_L^2}$$

$\hookrightarrow = 0$

Production energy threshold is: $E_{cm} = \sum_i m_i c^2$, $E_{kin} = 0$

E_{cm} grows with $E_L \rightarrow$ can produce higher masses

Summary: can produce **particles not contained in ordinary matter**

Example: Inelastic proton collisions

- We want to produce 3 protons and 1 antiproton colliding a proton beam against a proton target ($pp \rightarrow \bar{p}ppp$)
- What is the minimum momentum of the proton beam?
- Solution:
 - ◆ $m_1 = m_2 = 0.9383 \text{ GeV}/c^2$
 - ◆ $m(\text{anti-proton}) = m(\text{proton})$
 - ◆ $p_L = p_1, p_2 = 0$
 - ◆ At threshold: $E_{\text{CM}} = 4m = 3.7532 \text{ GeV}$
 - ◆ **Solving in p_1 : $p_1 = 6.5 \text{ GeV}/c$**

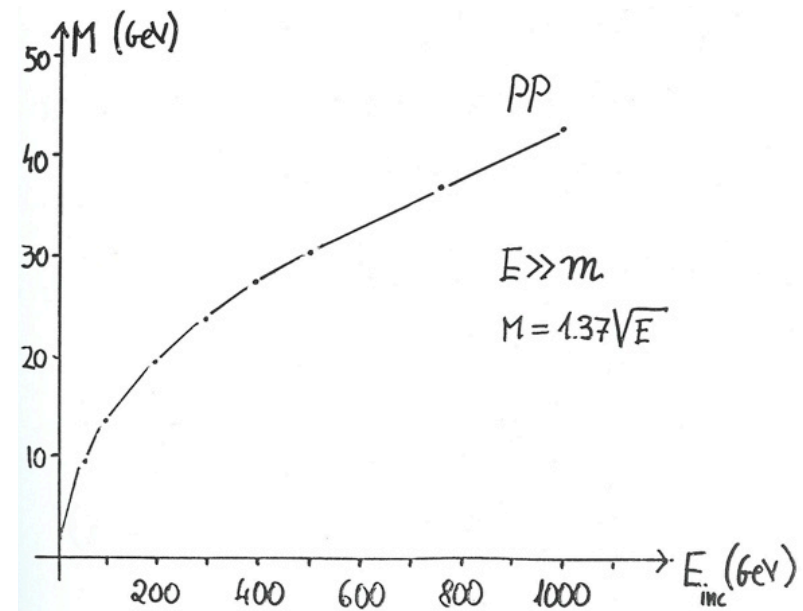
Center of mass energy

- As we have seen, E_{CM} is the energy available to generate mass
- In a beam-target collision E_{CM} grows slowly with the beam energy

$$E_L = \sqrt{p_L^2 + m^2} + m$$

$$M^2 = E_L^2 - p_L^2 = 2m^2 + 2m\sqrt{p_L^2 + m^2} \quad p_L = p_{inc}$$

$$p_{inc} \text{ large} \quad M \rightarrow \sqrt{2mp_{inc}} = 1.37\sqrt{p_{inc}} = 1.37\sqrt{E_{inc}}$$



Center of mass energy

- In beam-beam collisions: $E_{CM}=2xE_{beam}$
- Examples:
 - ◆ 22 GeV + 22 GeV has the same E_{CM} as 1 TeV+m_{target}
 - ◆ 1 TeV + 1 TeV has the same E_{CM} as 10^6 TeV+m_{target}
- Much more efficient to use two beams in opposite directions
- The concept naturally leads to the large circular accelerators
- Problem:
 - ◆ **Particle density** in a beam is much lower than **solid or liquid target**
- Solutions:
 - ◆ Cross beam many times
 - ◆ Maximize beam intensity (number of particle bunches per beam)
- Constraints:
 - ◆ Works only with stable (anti)particles (protons,electrons)
 - ◆ High vacuum needed to avoid beam-gas interactions: $\sim 10^{-9}$ Pa
 - ◆ particle-particle → circulate in two separate beam lines
 - ◆ particle-antiparticle → circulate in the same beam line, opposite directions

Acceleration methods

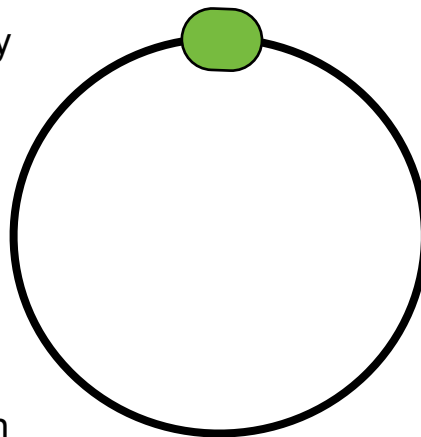
- **Can we use an electrostatic field?**
 - ◆ $F=qE$ → Energy transfer to a charged particle → Acceleration
 - ◆ Electrostatic field generated by potential difference (in Volts)
 - ◆ Maximal difference ~ 10 MV → Maximal energy ~ 10 MeV
 - ◆ But: Electrostatic field is conservative (i.e. line integral is zero)!
 - ◆ Cannot be used more than one time. Total energy transferred to the beam is null!
- **How about a variable electric field?**
 - ◆ Main idea: utilize several times a **small** but **variable** potential difference
 - ◆ Two possibilities: **circular machines** and **linear machines (LINACs)**

CIRCULAR ACCELERATOR:
At least one accelerating cavity

Particles **receive a Δ Energy**
at every turn.

Particles must be **in phase**
with accelerating potential

Need **magnetic field** to
keep the beam on circular path



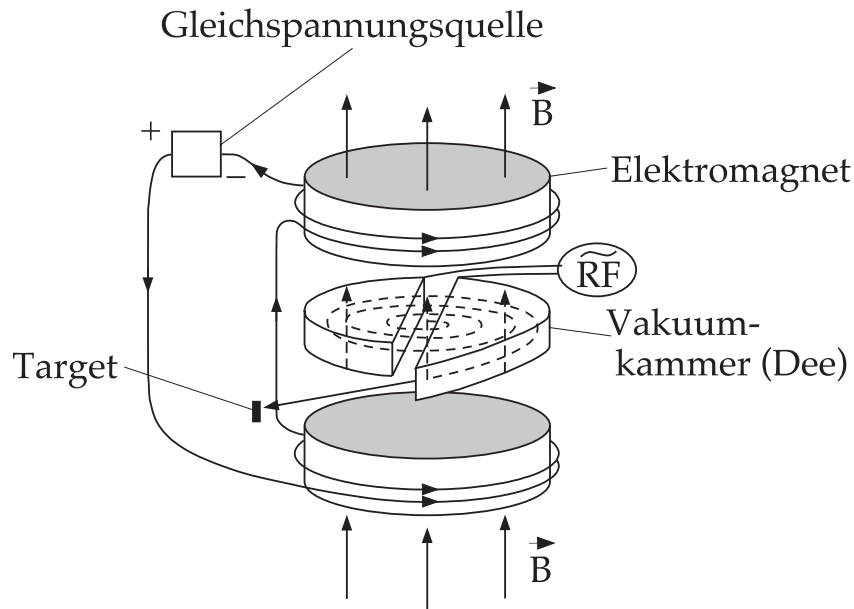
LINAC: multiple cavities



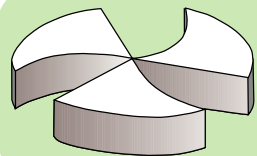
Particle accelerators: some history

- 1921: “Kaskadengenerator” (Greinacher)
- 1924-1928: Concept and first prototype of linear accelerator (Ising, Wideröe)
- 1932: First nuclear reaction induced by cascade particle accelerator, $p^7\text{Li} \rightarrow 2\alpha$ with 400 keV protons (Cockroft/Walton)
- 1930: First Van de Graaff accelerator with 1.5 MV
- 1930-1932: First 1.5 MeV cyclotron (concept: Lawrence)
- Upgraded cyclotrons (Synchrocyclotron): 300-700 MeV
- 1953: First synchrotron at Brookhaven lab - *Cosmotron* (concept: Oliphant/Veksler/McMillan): 3 GeV
- 1958: Proton Synchrotron (CERN): 28 GeV
- 1983: Tevatron (Fermilab): 1000 GeV
- 1990: HERA (DESY): first and only electron-proton collider
- 2008: Large Hadron Collider (CERN): up to 7000 GeV

Accelerators: Cyclotron



Maximal energy ~ 20 MeV
Synchro-cyclotron up to 600 MeV



Isochronous cyclotrons compensate the varying frequency by increasing the magnetic field with radius

- Centripetal force and Lorentz force are balanced:

$$m \frac{v^2}{\rho} = qvB.$$

- Cyclotron frequency:

$$v = \omega \rho \quad \omega = \frac{qB}{m}$$

- Alternating high voltage matches the cyclotron frequency
- The radius grows linearly with the impulse of the particle
- Cyclotron frequency for relativistic particles:

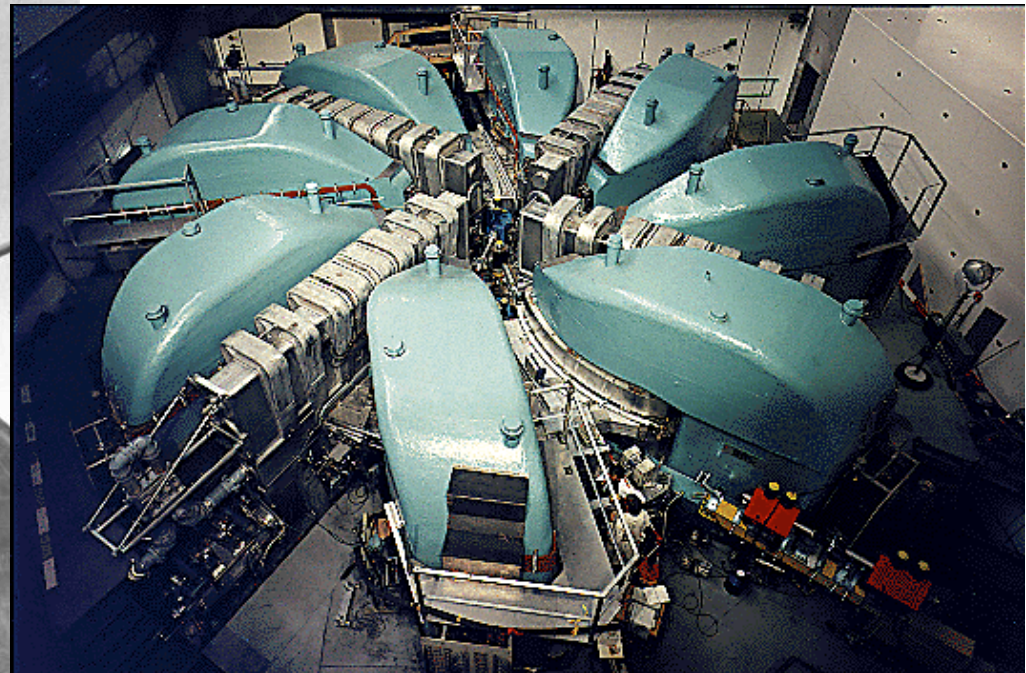
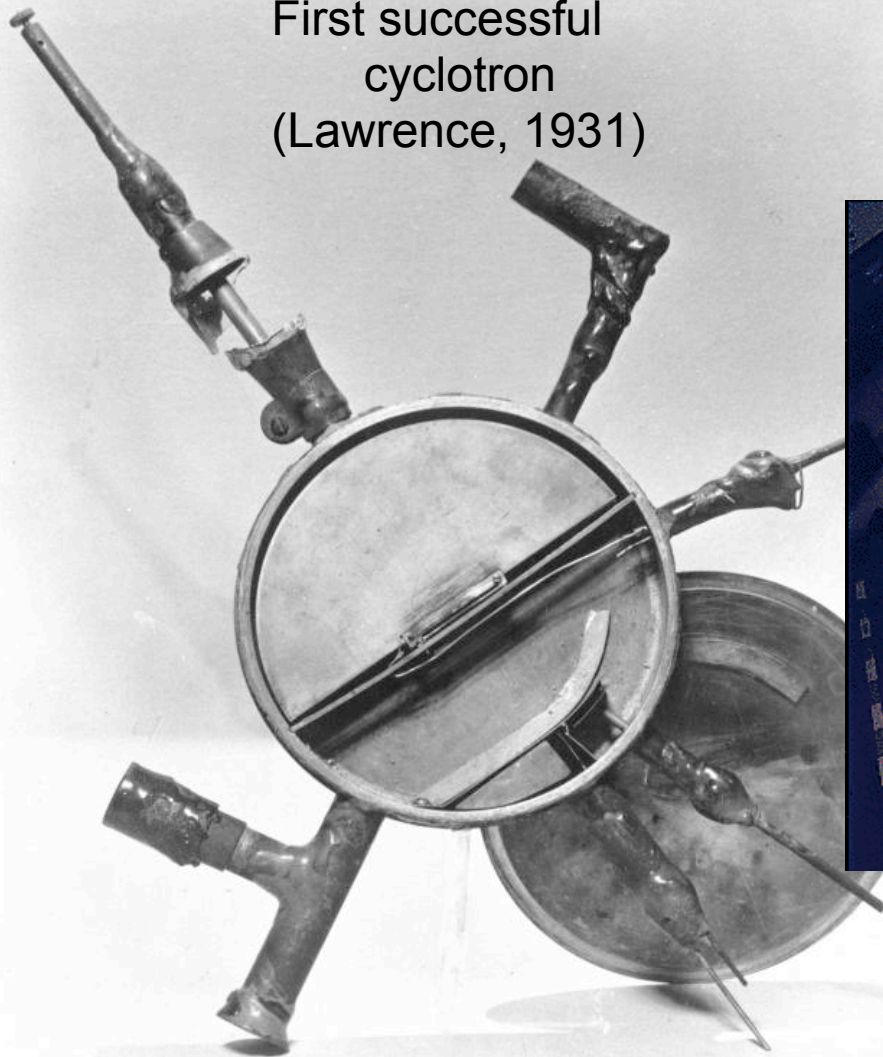
$$\omega = \frac{qB}{\gamma m}$$

$$v/c=50\%, \gamma=1.155, \omega'=0.86 \cdot \omega$$

$$v/c=99\%, \gamma=7.1, \omega'=0.14 \cdot \omega$$

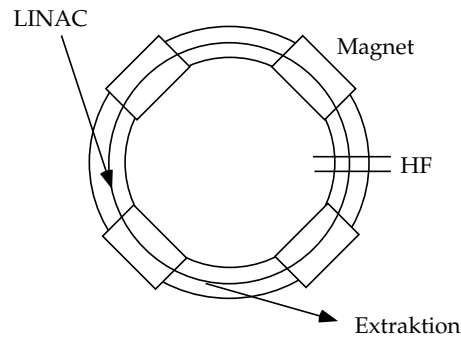
Cyclotrons

First successful
cyclotron
(Lawrence, 1931)

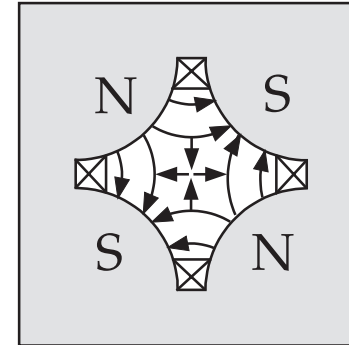
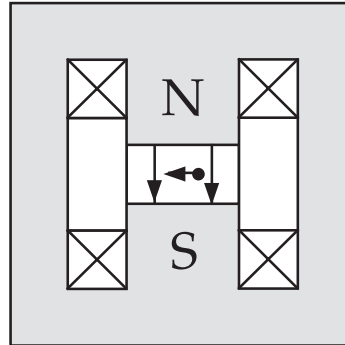


590 MeV cyclotron at the
Paul Scherrer Institut

Accelerators: Synchrotron



Dipole = Bending



Quadrupole = Focusing

- Momentum, B field and radius are related by:

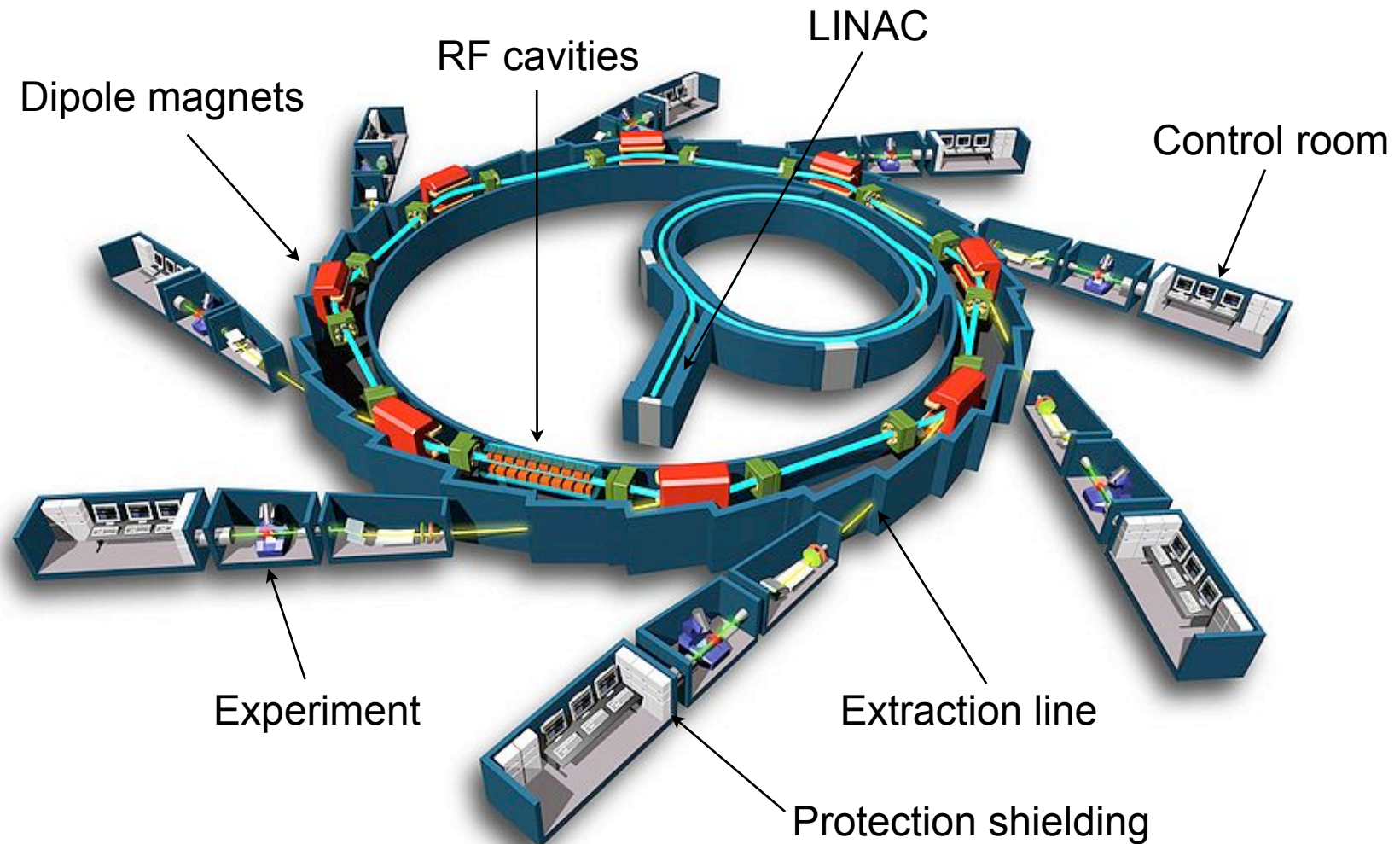
$$\rho = \frac{p}{qB}, \longrightarrow \begin{aligned} cp [\text{eV}] &= czB\rho = 3 \times 10^8 \text{ m} \cdot \text{s}^{-1} zB [\text{T}] \rho [\text{m}], \\ p [\text{GeV}/c] &= 0.3 z B [\text{T}] \rho [\text{m}] \end{aligned}$$

- Example: Large Hadron Collider:
 - Circumference: 27 Km → Radius = 4.3 Km
 - Average magnetic field = 5.4 Tesla
 - Momentum = 7 TeV/c for protons

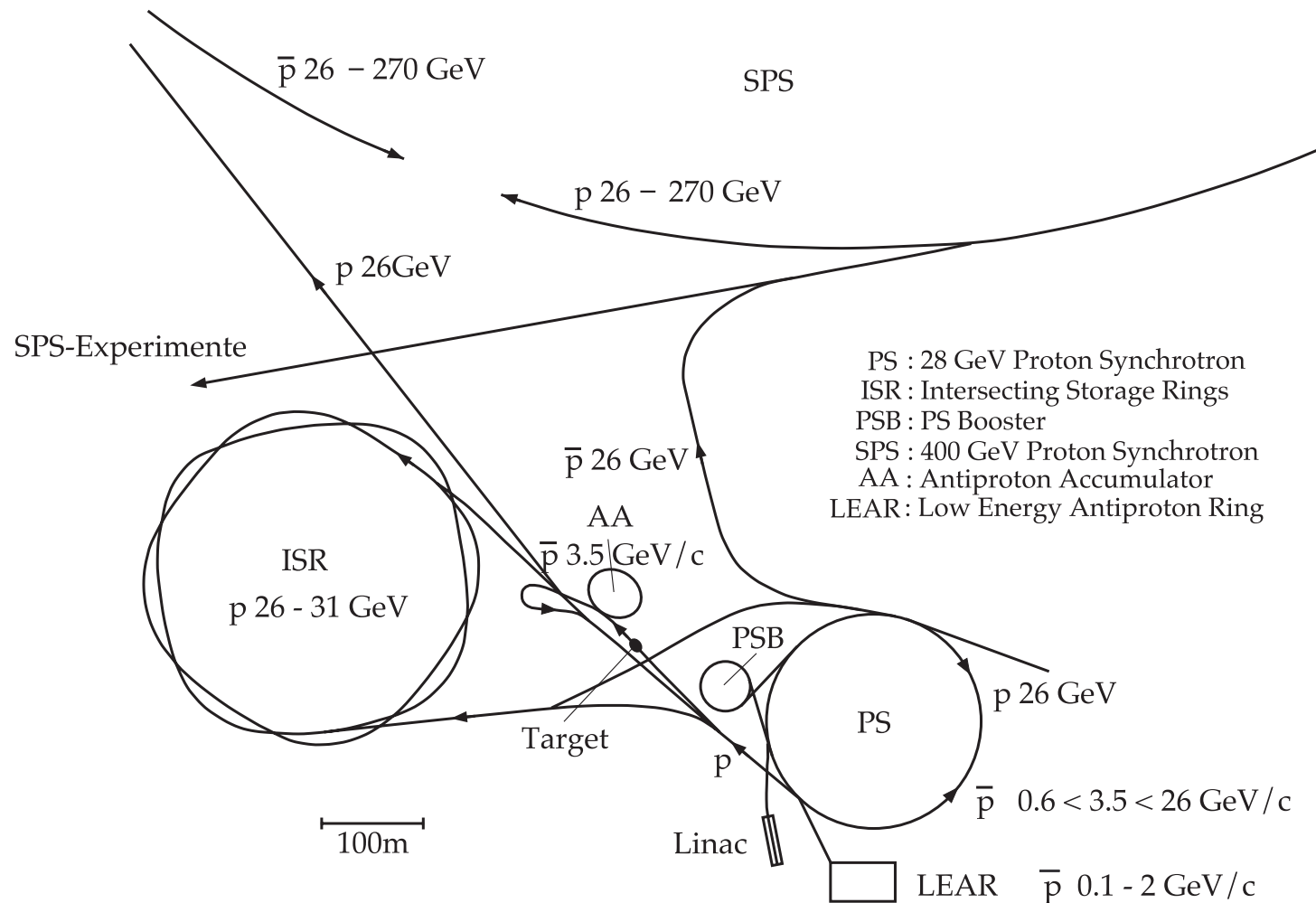
Synchrotron: main concepts

- Beams are injected at low energy with **B field** at its minimal value and particles move in a vacuum pipe
- At every turn the momentum grows:
 - ◆ To keep the beam on the same radius the B field has to grow accordingly
 - ◆ The revolution period also changes if the velocity grows
 - ◆ The potential difference (radio-frequency) must be kept in phase with the particles
- When the maximum momentum is reached the radio-frequency is switched off, then:
 - ◆ The beam can be extracted for experimental areas or to be injected in larger synchrotrons
 - ◆ The beams can be steered to meet in the collision points

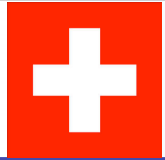
Synchrotron: a sketch



Accelerator complexes at CERN



The 450 GeV SPS beam is injected in the Large Hadron Collider



Swiss light source



- Location: Paul Scherrer Institut
- 2.8 GeV electron synchrotron
- 288 m circumference
- 36 dipoles, 1.4 T field
- 177 quadrupoles
- 100 MeV linear injector



Reminder: cross section

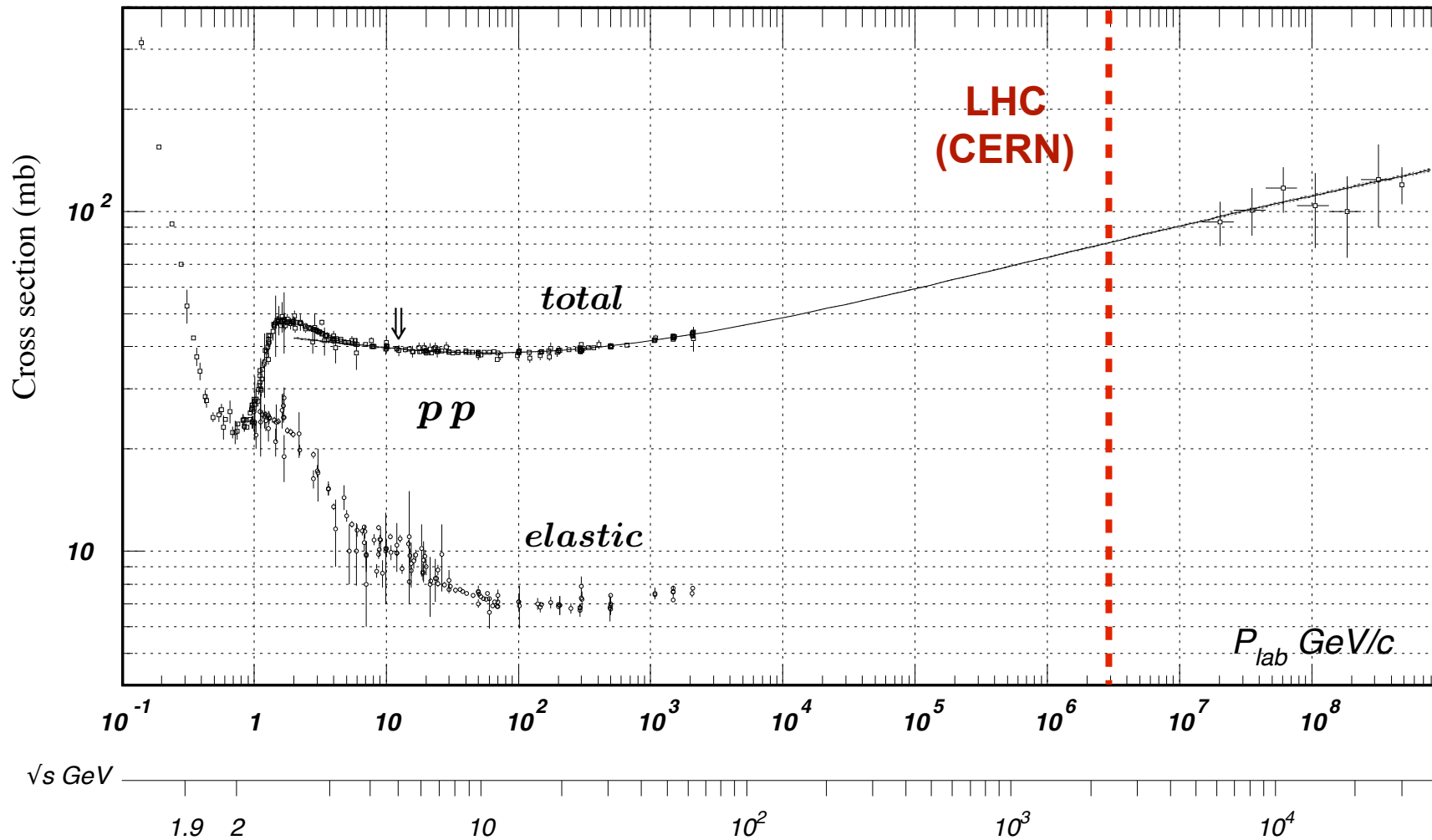
- Measured in cm^2 . The common unit is:

$$\text{barn} = 10^{-24} \text{ cm}^2 \quad [\text{b}]$$

- In the formulas used until now, we have used the total cross section (σ)
- The total cross section is the sum of many final states

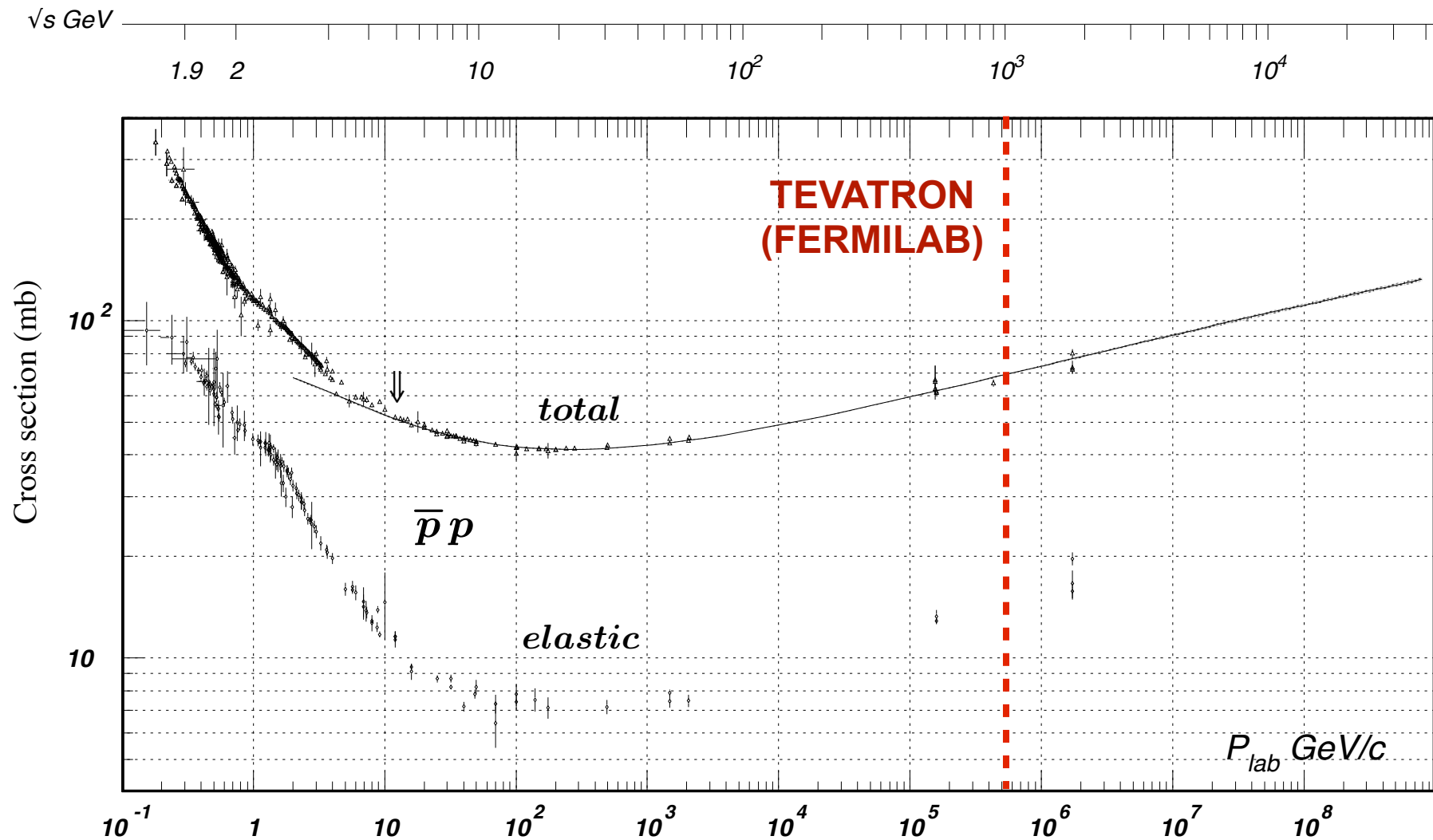
$$\sigma_{\text{TOT}} = \sum_i \sigma_i$$

Cross-sections: p-p



Source: <http://pdg.lbl.gov/2006/hadronic-xsections/hadron.html>

Cross sections: p-antip



Source: <http://pdg.lbl.gov/2006/hadronic-xsections/hadron.html>

Luminosity

- Cross section = σ
- Number of events per second = rate = R

$$R = L \sigma$$

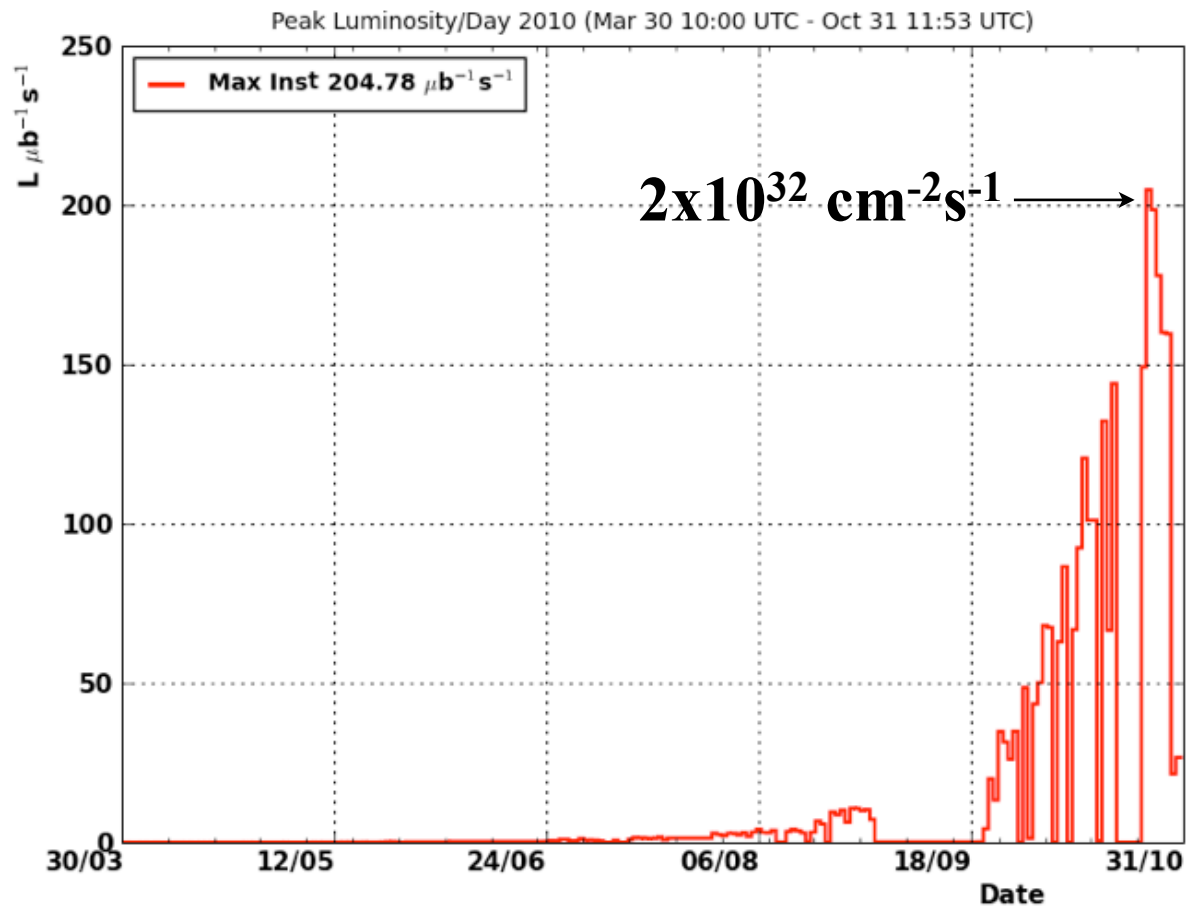
- L =Luminosity. Characterizes accelerator performances in [$\text{cm}^{-2}\text{s}^{-1}$]
- Example:
 - ◆ Consider a e^+e^- accelerator with N particles per beam turning f times per sec.
 - ◆ Gaussian shaped beam with dimensions σ_x and $\sigma_y \rightarrow$ transverse size = $4\pi\sigma_x\sigma_y$
 - ◆ One electron in one turn crosses $N/(4\pi\sigma_x\sigma_y)$ positrons
 - ◆ Number of **collisions** per second

$$\frac{fN^2}{4\pi\sigma_x\sigma_y}$$

- ◆ Number of **events** per second

$$R = \frac{\sigma f N^2}{4\pi\sigma_x\sigma_y}$$

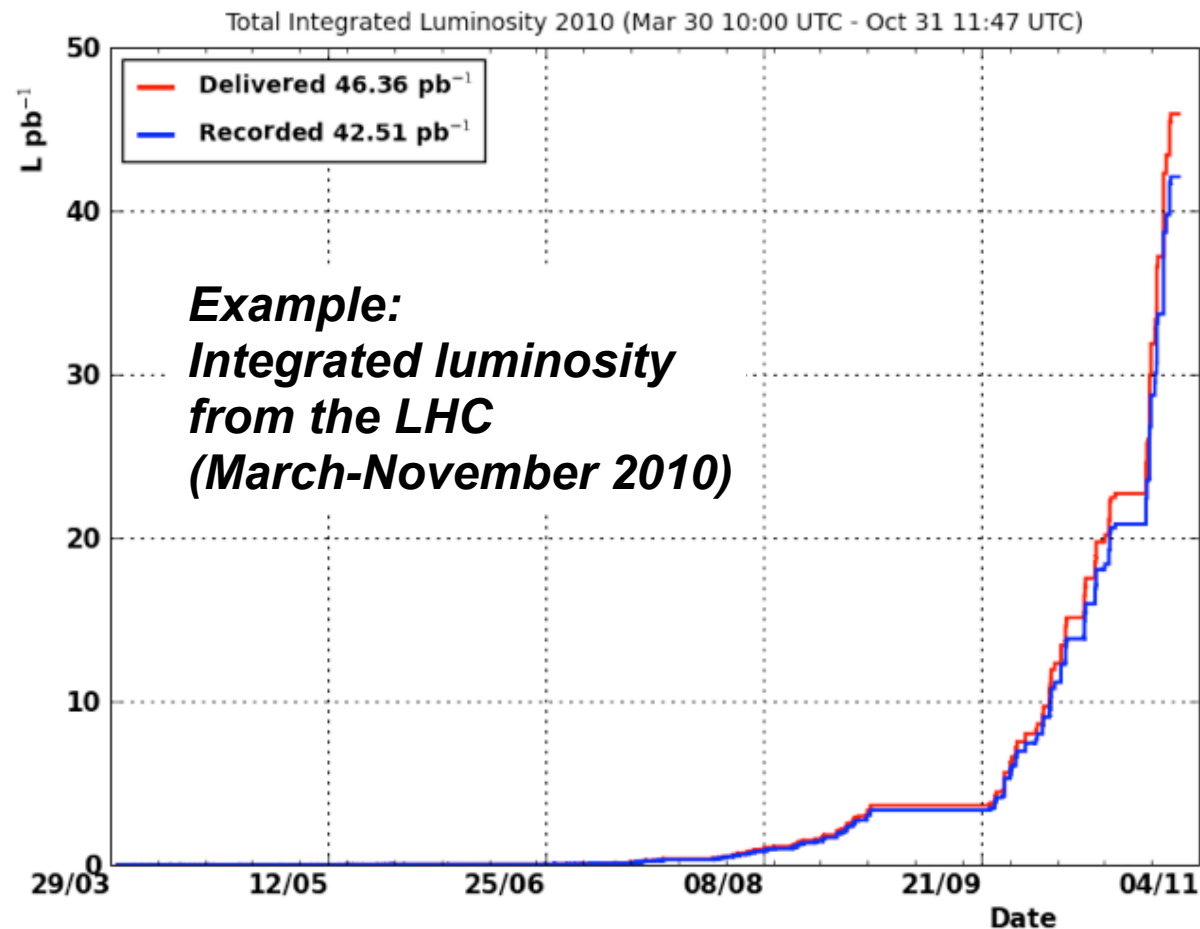
Instantaneous luminosity: LHC



- Accelerator luminosity is gradually increased by increasing the number of particles in the beam and squeezing the beam size at the intersection point
- Note: final target instantaneous luminosity for LHC is $10^{34} \text{ cm}^{-2}\text{s}^{-1}$

Integrated luminosity

- The integral of the delivered luminosity over time is called integrated luminosity
- The integrated luminosity is a measurement of the collected data size



Luminosity: example

■ Electron-Positron Accelerator ring:

- ◆ Ring is 100m long and revolution frequency is $f=3 \cdot 10^6$ Hz
- ◆ $N=10^{10}$ particles, $\sigma_x=0.1$ cm, $\sigma_y=0.01$ cm
- ◆ $L = 0.2 \times 10^{29} \text{ cm}^{-2}\text{s}^{-1}$

■ We are interested in a rare process:

- ◆ Example $e^+e^- \rightarrow \bar{p}p$ and $E_{\text{CM}} \sim 2-3$ GeV
- ◆ Cross section: $\sigma = 1 \text{ nb} = 10^{-33} \text{ cm}^2$
- ◆ $R=10^{-4}$ events per second
- ◆ ~ 0.35 events/hour
- ◆ ~ 8.5 events/day

Particle physics experiments

- Particle detectors are disposed around the interaction region and detect (directly or indirectly) the reaction products
- Typical measurements performed:
 - ◆ Spatial coordinates and timing of final state particle
 - ◆ Momentum: P_x , P_y , P_z
 - ◆ Energy
 - ◆ Type of particle (particle ID): pion, Kaon, proton, muon, etc.

Momentum measurement

- In high energy experiments the momentum measurement is based on the deflection of charged particles in a magnetic field

- Simple case:

- ◆ Dipole magnet
- ◆ Measure track direction before and after magnet

- In collider experiment:

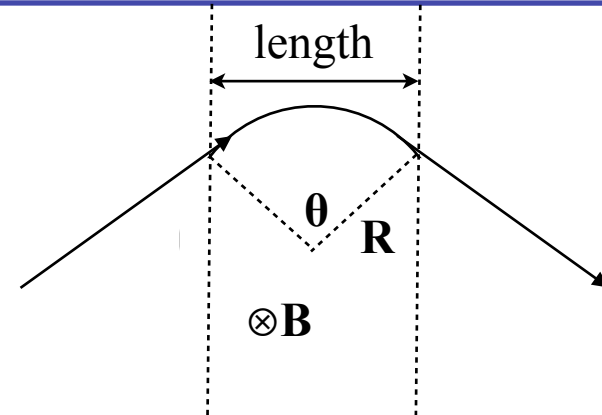
- ◆ B field parallel to beams
- ◆ Curvature only in the transverse plane
- ◆ Momentum resolution:

$$\frac{\sigma(p_T)}{p_T} = \frac{\sigma_{r\phi} p_T}{0.3 B l R^2} [720/(n+4)]^{-1/2}$$

$\sigma_{r\phi}$ = error on each measurement point

l_R = radial length of the track

n = number of equidistant points

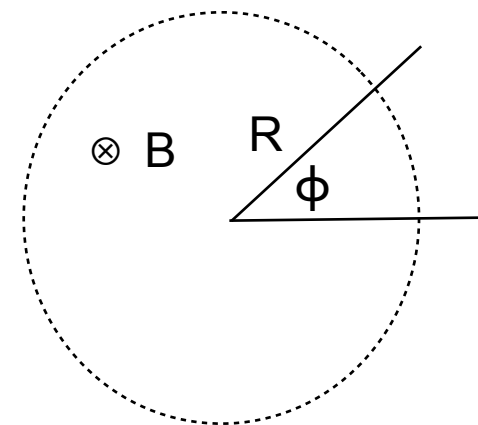


$$|p| = 0.3 |B| R$$

$$\text{length} = l = 2 R \sin(\theta/2) \sim R \theta$$

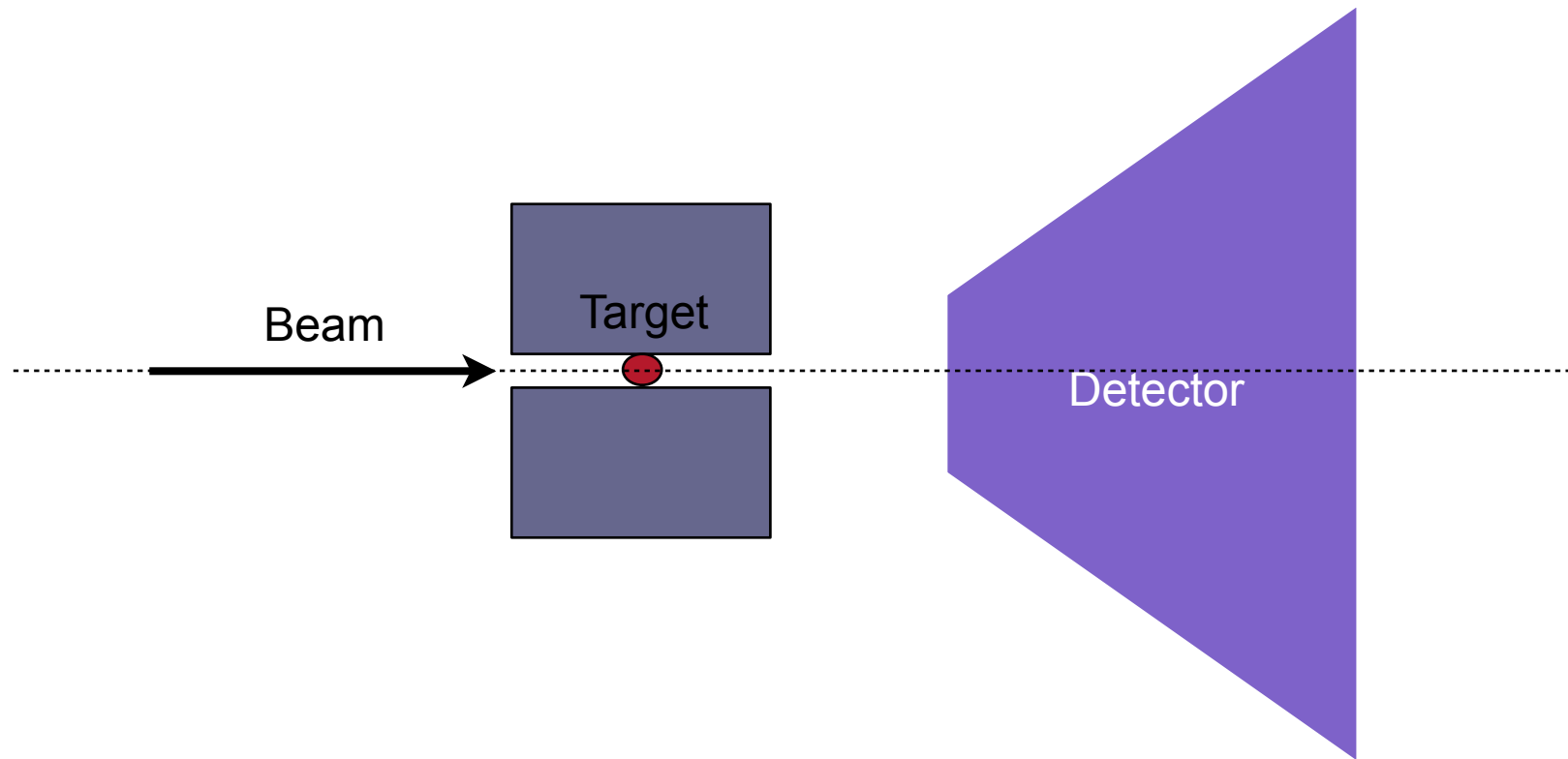
$$\theta = \text{length}/R = 0.3 B l / p$$

$$p = 0.3 B l / \theta$$

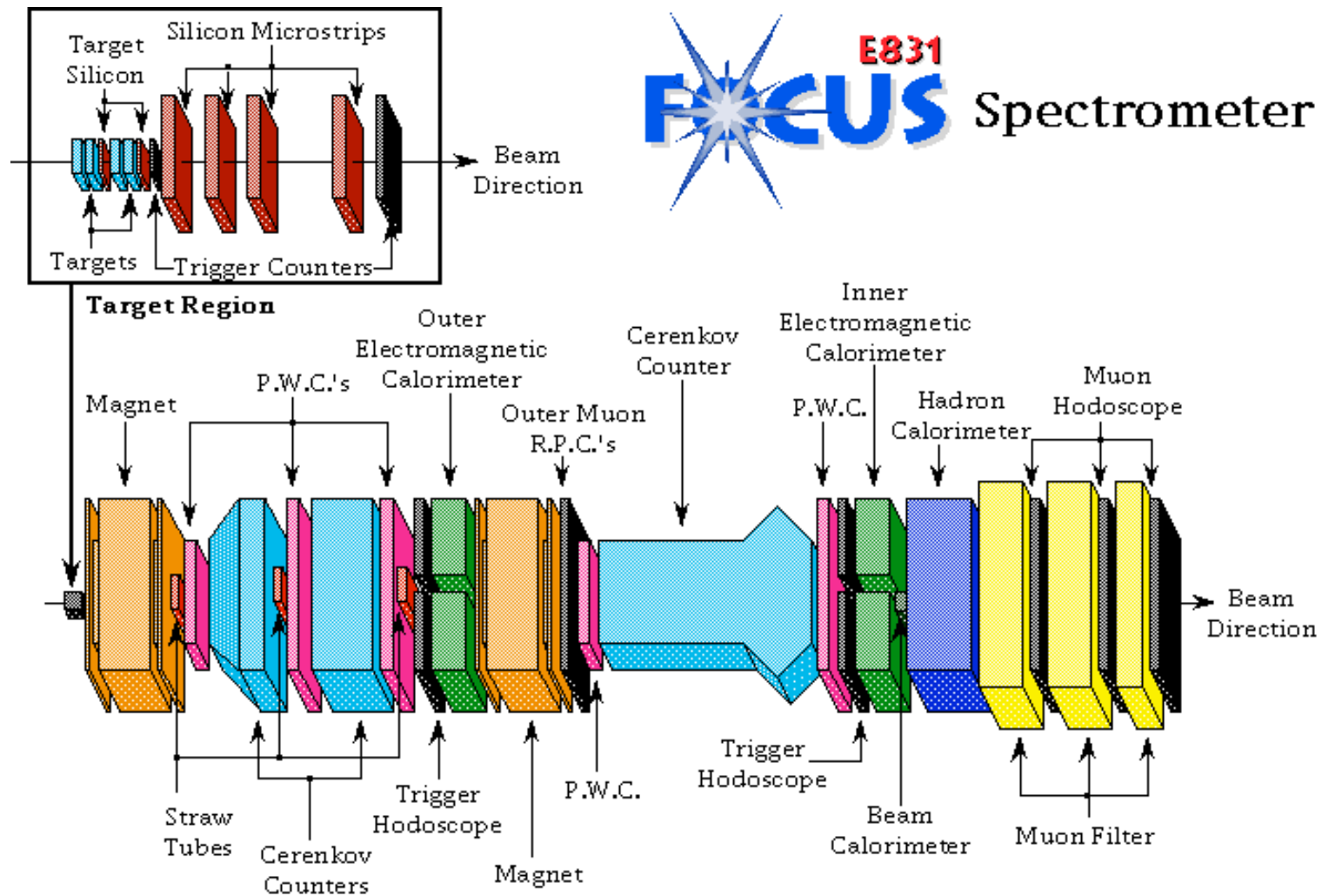


Fixed target experiments

- For fixed target experiments the production is essentially in the forward direction

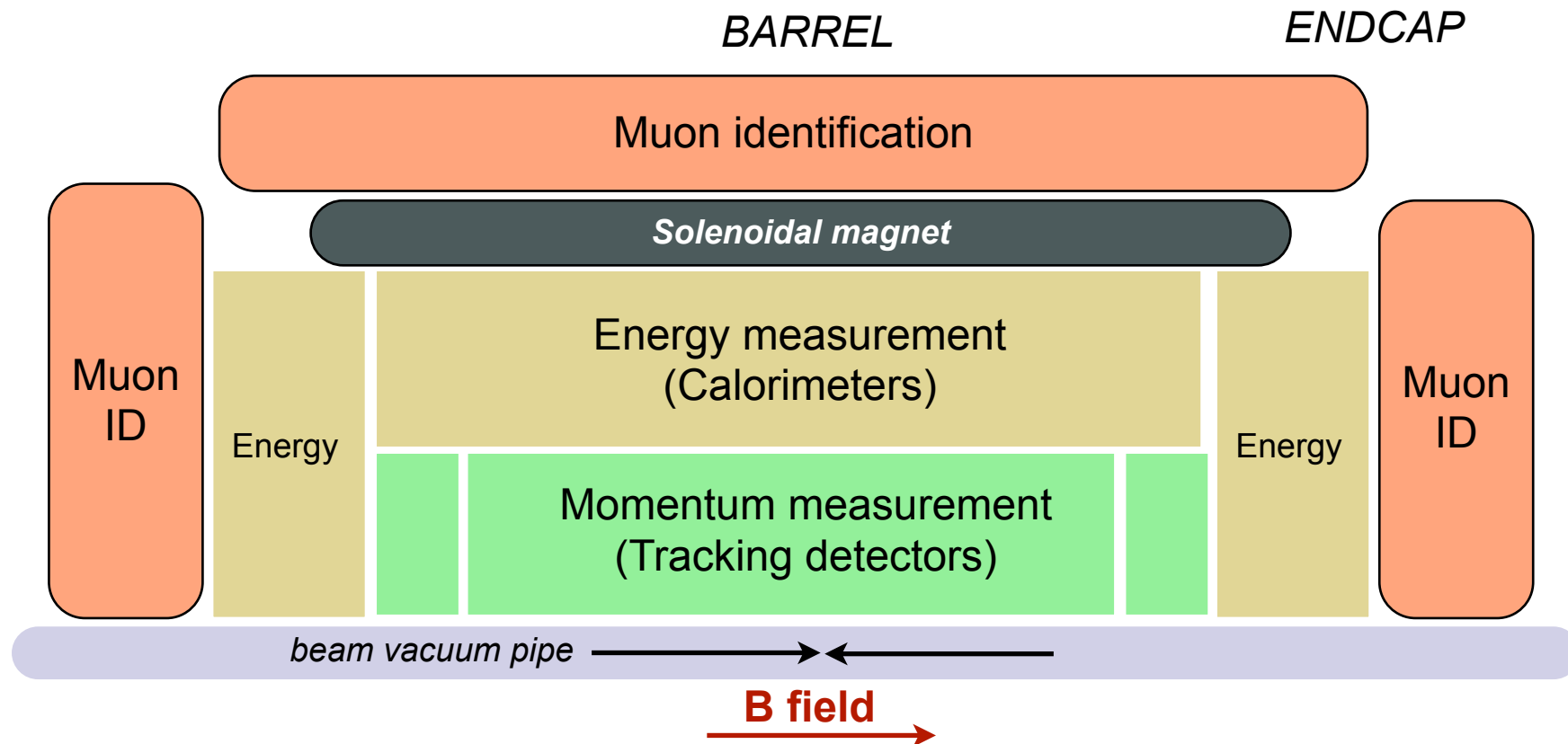


Example: FOCUS experiment



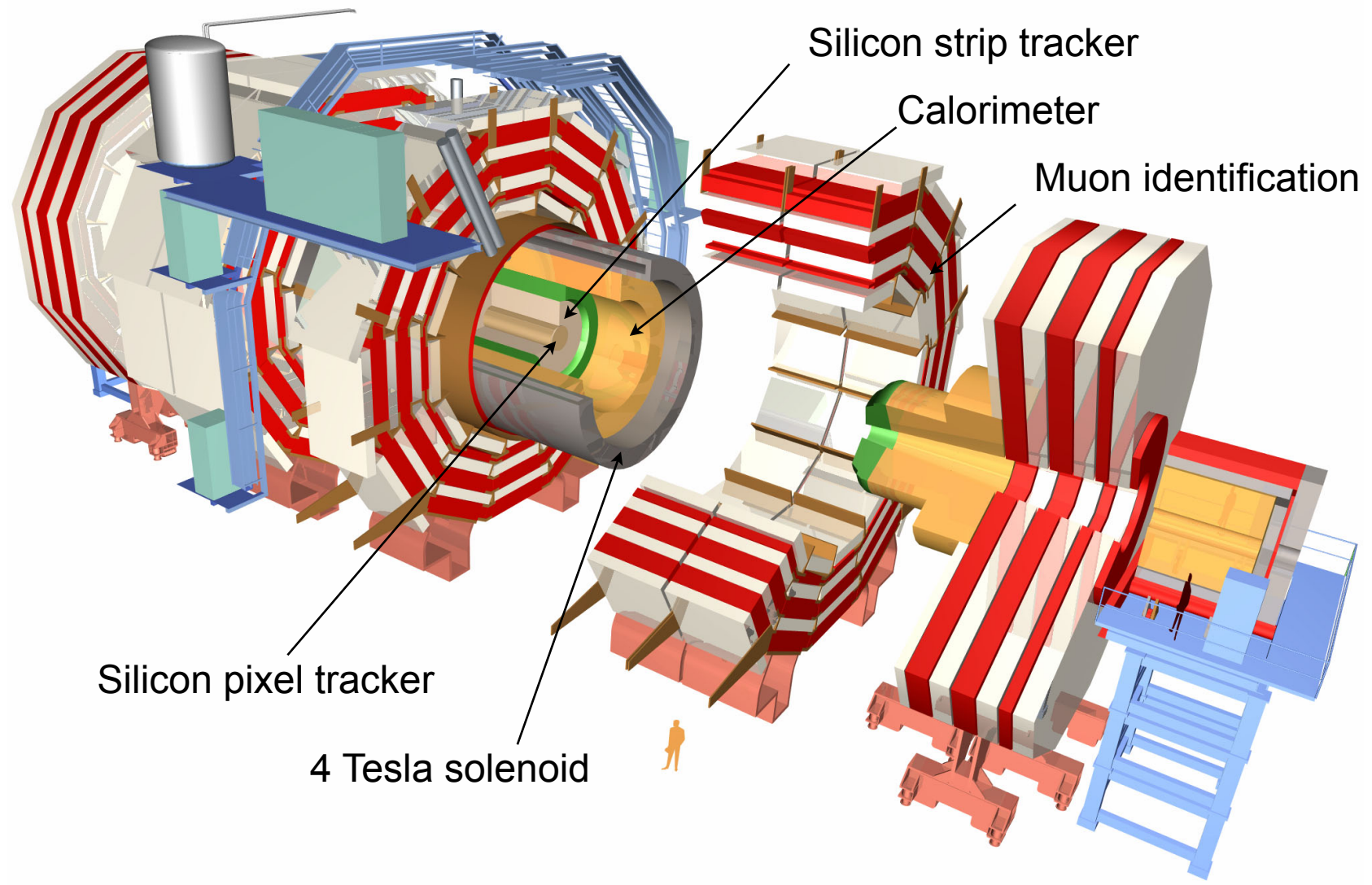
Collider experiments

- Cylindrical symmetry
- Ermeticity: measure as many of the final state particles as possible
- Magnetic field (solenoidal, \mathbf{B} parallel to the colliding beams)



Basic building blocks of a particle collider experiment

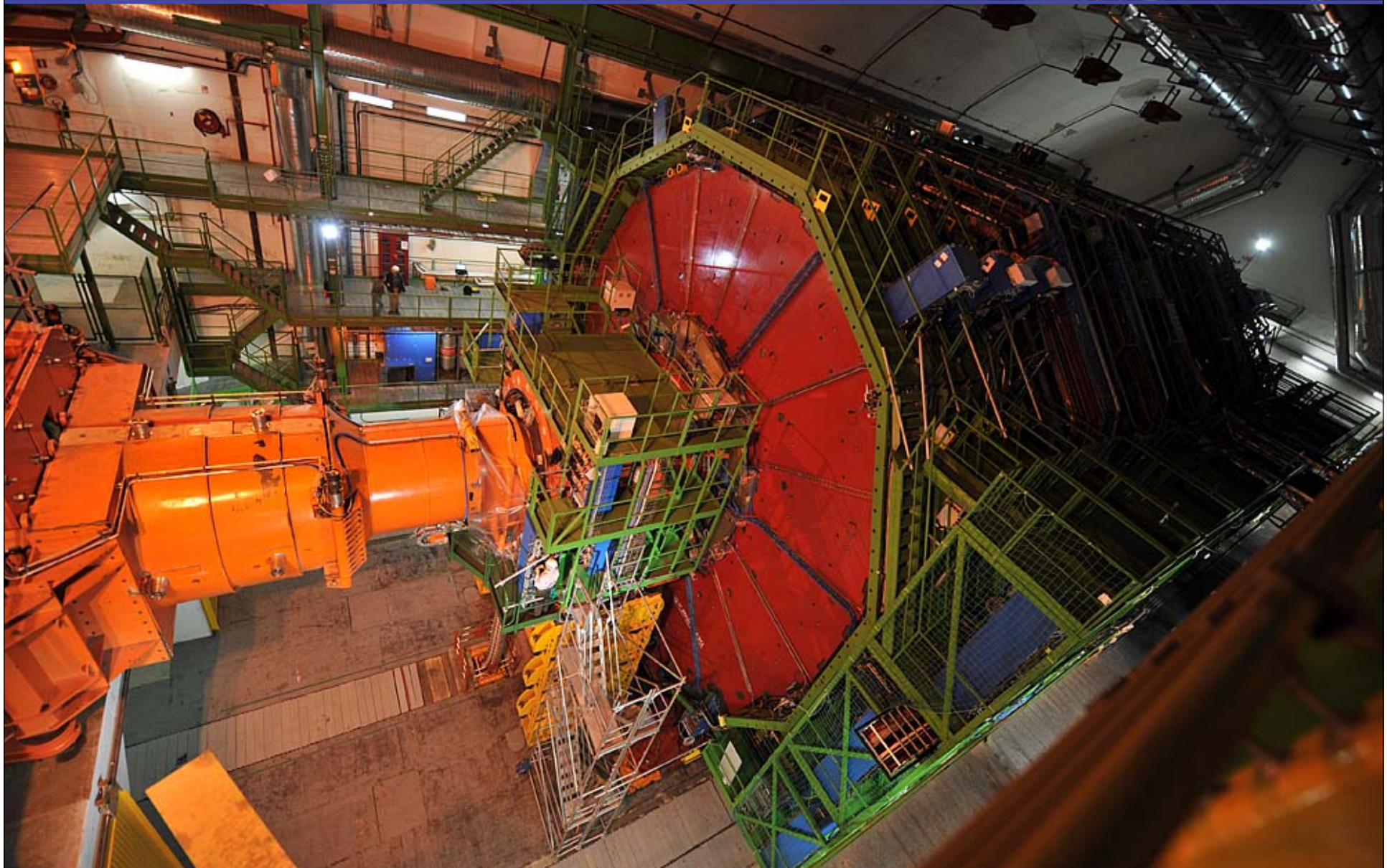
Example: CMS Experiment



CMS: open configuration



CMS: closed configuration



References

1. C.Amsler, *Kern- und Teilchenphysik*, UTB, 2007 (www.utb.de)
2. C.Grupen, B.Shwartz, *Particle Detectors*, Cambridge Univ. Press. 2008