

	Microcanonical ensemble	Canonical ensemble	Grand canonical ensemble
density (unrenormalized)	$\rho(p, q) = \delta(E - \mathcal{H}(p, q))$	$\rho(p, q) = e^{-\beta\mathcal{H}(p, q)}$	$\rho(p, q) = e^{-\beta(\mathcal{H}(p, q) - \mu N)}$ $= z^N e^{-\beta\mathcal{H}(p, q)}$
partition function	$Z_{\text{m'can}} = \Lambda_N \int dpdq \rho(p, q)$ $= \omega(E)$	$Z_N = \Lambda_N \int dpdq \rho(p, q)$ $= \Lambda_N \int dpdq e^{-\beta\mathcal{H}(p, q)}$	$\mathcal{Z} = \sum_{N=0}^{\infty} \Lambda_N \int dpdq \rho(p, q, N)$ $= \sum_{N=0}^{\infty} z^N Z_N$
average value	$\langle A \rangle = \frac{\Lambda_N}{\omega(E)} \int dpdq \rho(p, q) A(p, q)$	$\langle A \rangle = \frac{\Lambda_N}{Z_N} \int dpdq \rho(p, q) A(p, q)$	$\langle A \rangle = \sum_{N=0}^{\infty} \frac{\Lambda_N}{\mathcal{Z}} \int dpdq \rho(p, q, N) A(p, q, N)$
thermodyn. potential	$S(E, V, N) = k_B \log \omega(E, V, N)$	$F(T, V, N) = -k_B T \log Z_N(T, V)$	$\Omega(T, V, \mu) = -k_B T \log \mathcal{Z}(T, V, \mu)$